

# A comparison of different types of declarative modelling

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# Outline

- 1 Models and terminology
- 2 Conceptual data models
- 3 Ontologies
- 4 Conclusions

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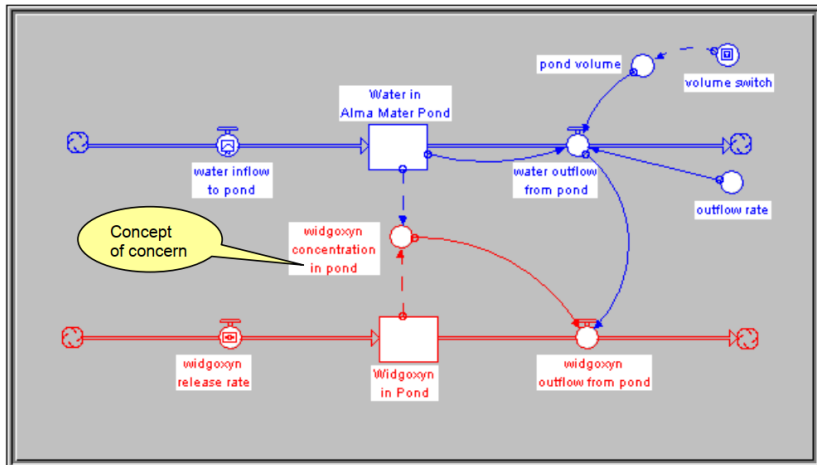
# Models galore

- Physical model; e.g., Lego brick house
- Mathematical model; e.g., climate change model, bacterial growth in cheese-making
- Machine learning & cs.; e.g., data-driven spellchecker, LLM
- Conceptual models; e.g., concept maps, UML diagrams, ontologies

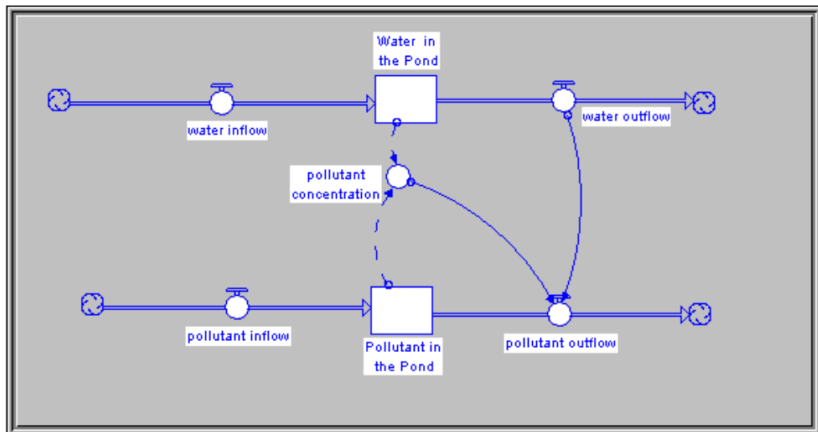
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- ⇒ Gentle, mostly non-technical introduction to conceptual models in computing, with a few half-baked props on 'things with water'

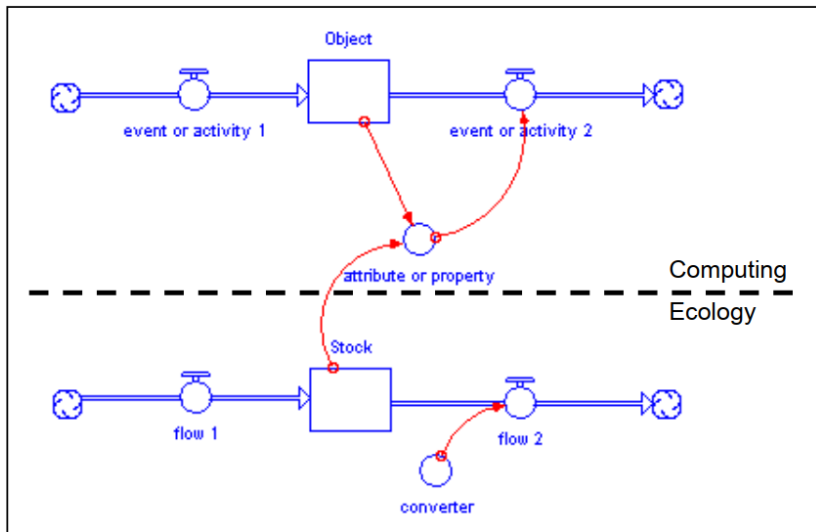
# An old TOY example – linking different perspectives



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## Matching things and terminology (1/2)

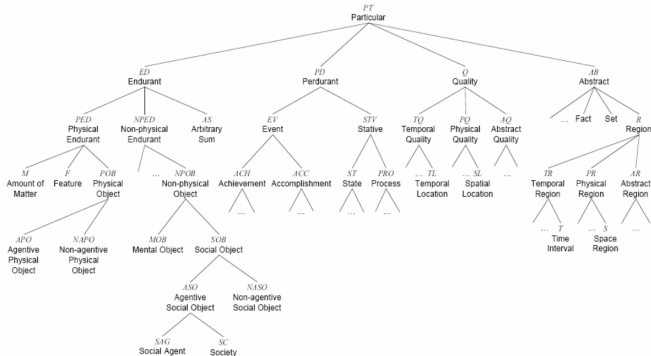
- *Stock* typically named with a noun (particular or universal)
- *Flow* named with a verb
- *Converter* as an attribute related to Flow or Stock
- *Action Connector* relates the former
- *Object* is candidate for an endurant
- *Event\_or\_activity* for a method or perdurant
- *Converter* maps to attribute\_or\_property
- *Action Connector* candidate for relationship between any two of Flow, Stock and Converter

---

More information and evaluation (with the microbial loop in ocean): Keet CM. Factors affecting ontology development in ecology. DILS'05.

# Matching things and terminology (1/2)

- $\forall x(Stock(x) \rightarrow EnDurant(x))$
- $\forall x(Flow(x) \rightarrow PerDurant(x))$
- $\forall x(Converter(x) \rightarrow (Quality(x) \vee State(x)))$
- $\forall x(ActionConnector(x) \rightarrow Relationship(x))$



## Some questions (part 1)

- Stella is rather outdated; which other (declarative) modelling languages could this be done with?
- What to convert it into?
  - Domain specific language
  - Conceptual data model, process model, ...
  - More generic terminology, classes, relations, and constraints (an ontology?)

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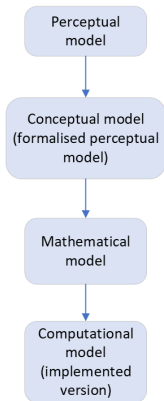
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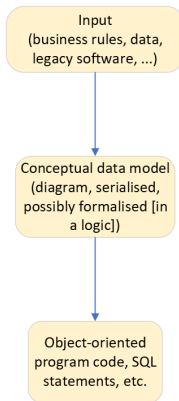
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- Why even do this?
  - integrating models, comparing models, checking for possible inconsistencies automatically
  - Management of the mathematical models: separate declarative from the imperative

# Terminology, simplified processes, and some links

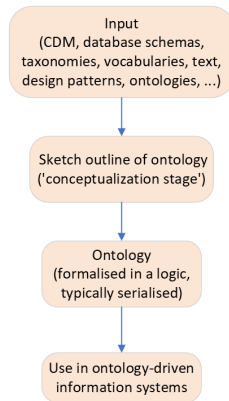
**Hydrological model development**  
 (conceptual, physical, and data-driven)



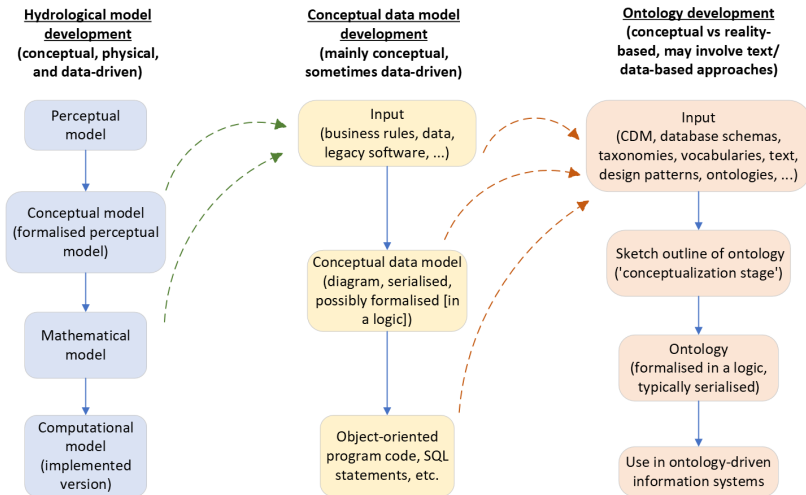
**Conceptual data model development**  
 (mainly conceptual, sometimes data-driven)



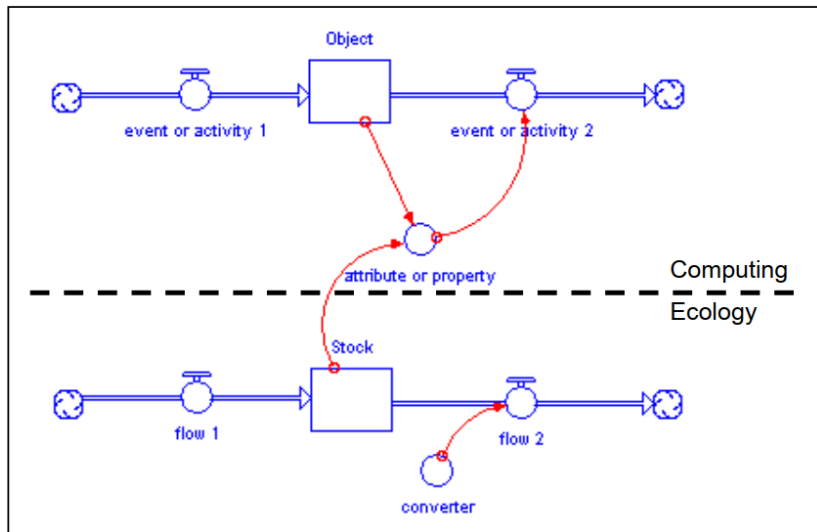
**Ontology development**  
 (conceptual vs reality-based, may involve text/data-based approaches)



# Terminology, simplified processes, and some links











# On the maths – scaffold generation

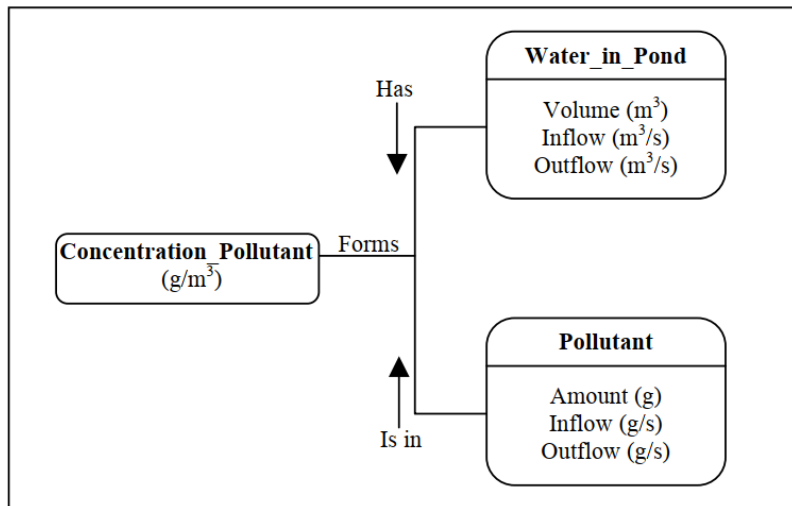




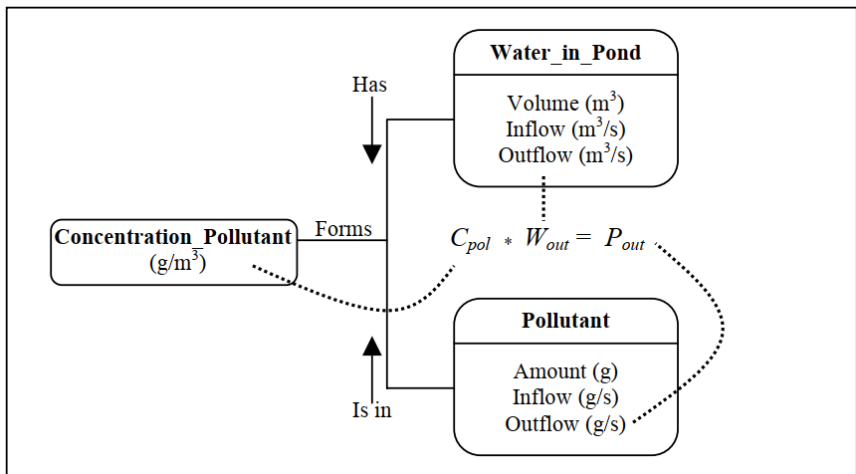
# On the maths – scaffold generation

-  Object(t) = Object(t - dt) + (event\_or\_activity\_1 - event\_or\_activity\_2) \* dt  
INIT Object = { Place initial value here... }  
INFLOWS:  
 event\_or\_activity\_1 = { Place right hand side of equation here... }  
OUTFLOWS:  
 event\_or\_activity\_2 = { Place right hand side of equation here... }
-  Stock(t) = Stock(t - dt) + (flow\_1 - flow\_2) \* dt  
INIT Stock = { Place initial value here... }  
INFLOWS:  
 flow\_1 = { Place right hand side of equation here... }  
OUTFLOWS:  
 flow\_2 = { Place right hand side of equation here... }
-  attribute\_or\_property = { Place right hand side of equation here... }
-  converter = { Place right hand side of equation here... }

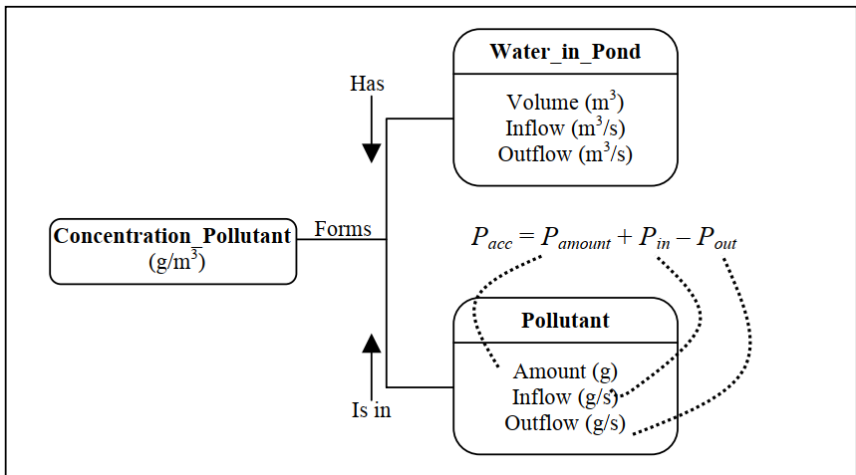
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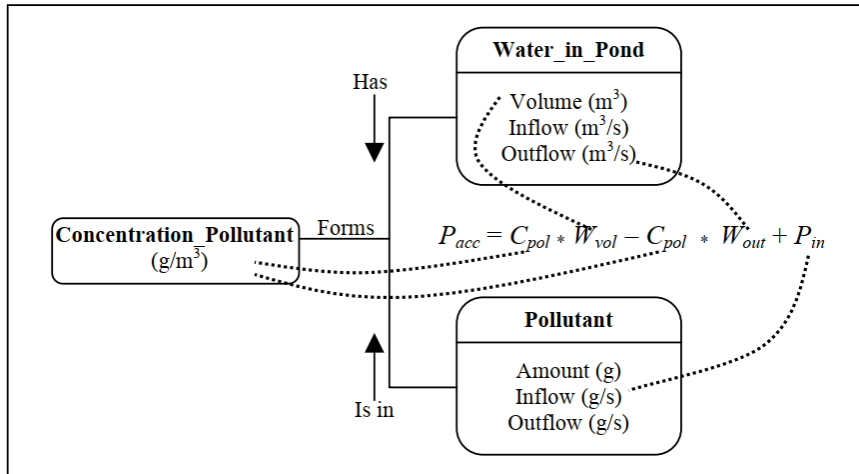
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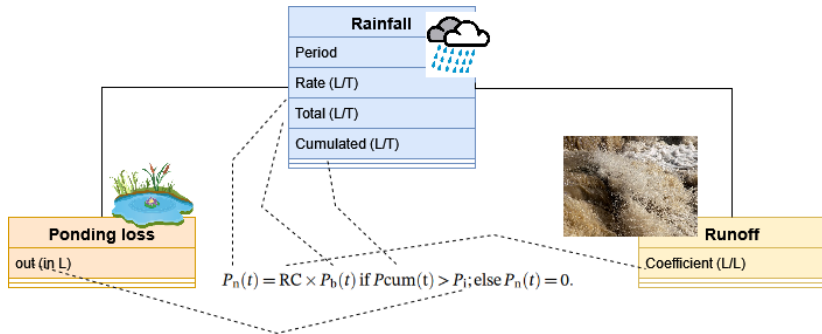
# On the maths – scaffold generation



# On the maths – scaffold generation



# On the maths – a recent paper



formula from: Chahinian N, et al. (2023). Evaluation of an early flood warning system in Bamako (Mali): Lessons learned from the flood of May 2019. J Flood Risk Mgmt.

## Some questions (part 2)

- How to do something like this systematically?
- Will any of the current applied maths markup languages (e.g., SBML) suffice?

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- How to do something like this systematically?
- Will any of the current applied maths markup languages (e.g., SBML) suffice?
- Why look into this?
  - Annotation (declarative representation) of the formula separates the what (the formulae) from the how (the code how to compute it)
  - One declarative formula/model can be loaded 'trivially' across programming languages and executed
  - (Parts of) The declarative formula/model can more easily be reused, saving design time, facilitating interoperability

# SBML: random example of an SBML model from the BioModels database

## BIOMD0000000531\_url.xml

```
136 <listOfUnitDefinitions>
137 <unitDefinition id="volume" metaid="_224f94f3-7d8c-4058-899c-ef158671d01e" name="volume">
138   <listOfUnits>
139     <unit exponent="1" kind="litre" metaid="b0b05891-9c17-4104-836c-e37a86b35f95" multiplier="1" scale="-3"/>
140   </listOfUnits>
141 </unitDefinition>
142 <unitDefinition id="time" metaid="_45409b69-6247-4659-b564-97ab08e0e5cd" name="time">
143   <listOfUnits>
144     <unit exponent="1" kind="second" metaid="e38bd50b-5dda-4daa-a633-c6f6c51d2ed8" multiplier="3600" scale="0"/>
145   </listOfUnits>
146 </unitDefinition>
147 <unitDefinition id="substance" metaid="_7abe9aca-312c-4b5d-baa2-c64840864da1" name="substance">
148   <listOfUnits>
149     <unit exponent="1" kind="mole" metaid="_5aa1de13-c181-4205-a36f-9fbe53894ab3" multiplier="1" scale="-3"/>
150   </listOfUnits>
151 </unitDefinition>
```

# SBML: random example of an SBML model from the BioModels database

## BIOMD0000000531\_url.xml

```

196 <listOfParameters>
197 <parameter constant="true" id="Ka" metaid="COPASI2" name="Ka" value="1.44">
198 <annotation>
199 <COPASI xmlns="http://www.copasi.org/static/sbml">
200 <rdf:RDF xmlns:dcterms="http://purl.org/dc/terms/" xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#">
201 <rdf:Description rdf:about="#COPASI2">
202 <dcterms:created>
203 <rdf:Description>
204 <dcterms:W3CDTF>2014-07-17T15:42:40Z</dcterms:W3CDTF>
205 </rdf:Description>
206 </dcterms:created>
207 </rdf:Description>
208 </rdf:RDF>
209 </COPASI>
210 </annotation>
211 </parameter>
212 <parameter constant="true" id="kb" metaid="COPASI3" name="kb" value="1.6E-10">
213 <annotation>

```

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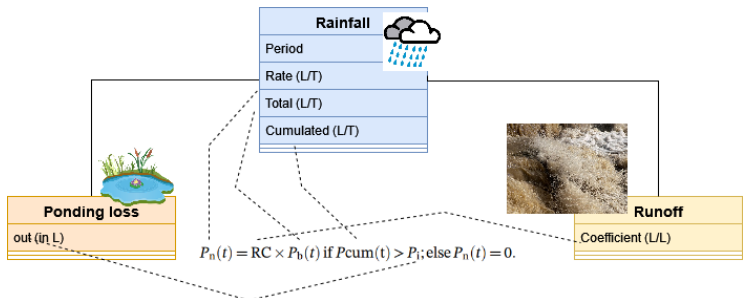
258     <listOfRules>
259       <assignmentRule metaid="_15d0c074-0652-4ed7-b795-9a1fd1a61655" variable="kat50">
260         <math xmlns="http://www.w3.org/1998/Math/MathML">
261           <apply>
262             <ln/>
263             <apply>
264               <plus/>
265               <apply>
266                 <divide/>
267                 <cn> 1 </cn>
268                 <ci> kb </ci>
269               </apply>
270             <cn> 1 </cn>
271           </apply>
272         </math>
273       </assignmentRule>
274       <assignmentRule metaid="d9080aa4-e7cc-4a7a-b7f7-b7ae59435fh4" variable="v50+50">
275

```

## Limitations of the domain models

- There are very many notations to learn
- Objects and arrows, but no way to specify how many outgoing arcs there may be
- Limited computational use among models
- Proliferation of incompatible modelling tools that are cumbersome to maintain

# Rainfall questions – loose ends in the model



- What are the names of the relations? the constraints? The relevant attributes? And their data types?

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# Solutions to limitations of the domain models

- Devise one notation for all
- More expressive (more features) than only objects and arrows
- Computational support
- (Try to) Standardise to make tooling development 'economically' viable



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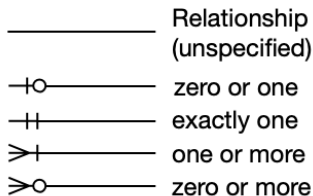
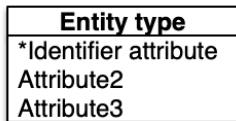
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- ⇒ Conceptual data models

# Conceptual data models

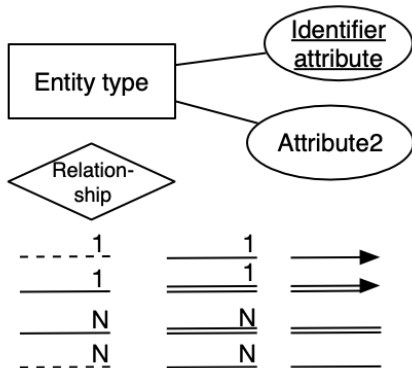
- A class of models that capture the information about the data that are to be stored in the prospective software system (and possibly manipulated)
- There are several conceptual data modelling language families and notations

# Conceptual data models – Example of language elements

## A. Crow's feet notation



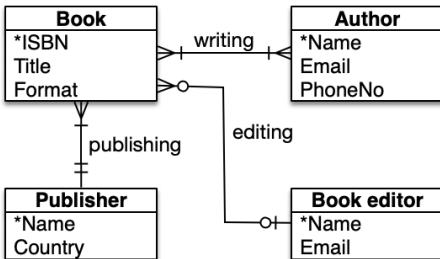
## B. Chen's notation



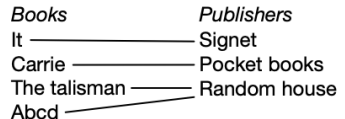
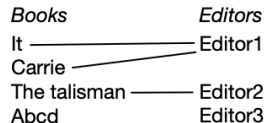
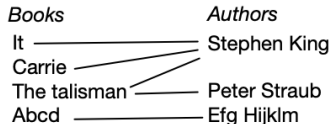
Note: no 'stock', 'flow' etc, but type of element for any subject domain

# Conceptual data models – Example

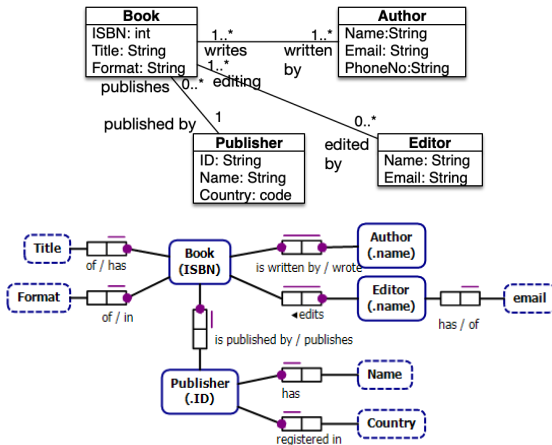
A. ER diagram using crow's feet notation



B. Population examples

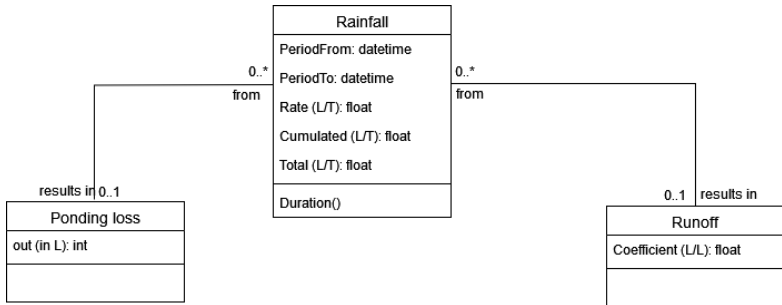


# Same example in UML and ORM



Convert automatically between EER, UML, ORM, choose preferred notation: Braun G, Fillotrani PR, Keet CM. A Framework for Interoperability Between Models with Hybrid Tools, J of Intell. Inf. Sys. 2023.

# Rainfall, again — UML style



- Convert UML class diagram (semi-)automatically into program code
- Easier to communicate with other domain experts and programmers what's in the code
- Easier to reuse with other math formula that use same entities

# Limitations of conceptual data model models in theory or practice

- For one specific application only – need to re-do it for each application, integration issues
- Solutions to recurring modelling issues re-invented time and again (and same mistakes made)
- Mostly informal diagrams that suffer from ambiguity (intentionally or not)
- Limited authoring guidelines<sup>1</sup>
- Some quality control mechanisms

---

<sup>1</sup> Mainly the CSDP for ORM [Halpin(2001)]; an example for EER: <http://www.meteck.org/modellingbook/DanceSchoolExample.html>; TDD proposal for UML [Tort and Olivé(2010)]

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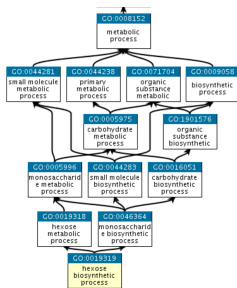


# Solving limitations of conceptual data model models with ontologies

- Model for a subject domain, of use across multiple applications for use, reuse, integration
- Provides solutions to recurring modelling issues, saves re-inventing
- Logic-based, as precise as permitted within the language
- Multiple quality control mechanisms (theories, methods, techniques, tools)

# An ontology...

Simplified graphical rendering of a fragment of most popular one:



(informally) *an* ontology is an engineering artefact in machine-processable format, which contains the entity types, their relationships, and constraints that hold over them of a particular (subject) domain.

<http://geneontology.org/docs/ontology-documentation/>

# In an ontology development environment (ODE)...

The screenshot displays the AfricanWildlifeOntology1 interface. The browser address bar shows the URL: <http://www.meteck.org/teaching/ontologies/AfricanWildlifeOntology1.owl...>. The main navigation bar includes tabs for Classes, Object Properties, Data Properties, Annotation Properties, Individuals, and OWLviz. The left pane shows a class hierarchy for 'lion', with 'lion' selected. The right pane shows annotations and descriptions for 'lion'. The annotations section includes a comment: "Lions are animals that eat only herbivores." The description section shows that 'lion' is equivalent to 'animal' and is a subclass of 'animal', 'eats only herbivore', and 'eats some Impala'. The bottom status bar indicates "No Reasoner set. Select a reasoner from the Reasoner menu" and a checked "Show Inferences" option.

AfricanWildlifeOntology1 (http://www.meteck.org/teaching/ontologies/AfricanWildlifeOntology1.owl...)

AfricanWildlifeOntology1 Search for entity

Classes Object Properties Data Properties Annotation Properties Individuals OWLviz

Class hierarchy Class hierarchy (inferred)

Class hierarchy: lion

- Thing
  - animal
    - carnivore
    - giraffe
    - herbivore
      - Elephant
      - Impala
      - lion
      - Omnivore
      - RockDassie
      - Warthog
    - Distribution
    - Habitat
    - plant
      - CarnivorousPlant
      - Grass
      - Palmtree

Annotations Usage

Annotations: lion

Annotations +  
comment  
Lions are animals that eat only herbivores.

Description: lion

Equivalent To +  
animal

SubClass Of +  
animal  
eats only herbivore  
eats some Impala

SubClass Of (Anonymous Ancestor)

No Reasoner set. Select a reasoner from the Reasoner menu  Show Inferences

## ... happenings behind the GUI ...

AfricanWildlifeOntology1 (http://www.meteck.org/teaching/ontologies/AfricanWildlifeOntology1.owl...)

AfricanWildlifeOntology1 Search for entity

Classes Object Properties Data Properties Annotation Properties Individuals OWLViz

Class hierarchy Class hierarchy (inferred)

Class hierarchy: lion

Annotations Usage

SubClassOf(awo:lion awo:animal)  
SubClassOf(awo:lion ObjectSomeValuesFrom(awo:eats awo:Impala))  
SubClassOf(awo:lion ObjectAllValuesFrom(awo:eats awo:herbivore))

SubClassOf

animal  
eats **only** herbivore  
eats **some** Impala

SubClass Of (Anonymous Ancestor)

No Reasoner set. Select a reasoner from the Reasoner menu  Show Inferences

## ... and underlying that serialisation

AfricanWildlifeOntology1 (http://www.meteck.org/teaching/ontologies/AfricanWildlifeOntology1.owl...)

AfricanWildlifeOntology1 Search for entity

Classes Object Properties Data Properties Annotation Properties Individuals OWLViz

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Annotations Usage

Annotations: lion

Annotations +  
comment  
Lions

Descriptions

Equivalent To +

SubClass Of +

- animal
- eats **only** herbivore
- eats **some** Impala

SubClass Of (Anonymous Ancestor)

Lion ⊆ Animal  
Lion ⊆ ∇eats.Herbivore  
Lion ⊆ ∃eats.Impala

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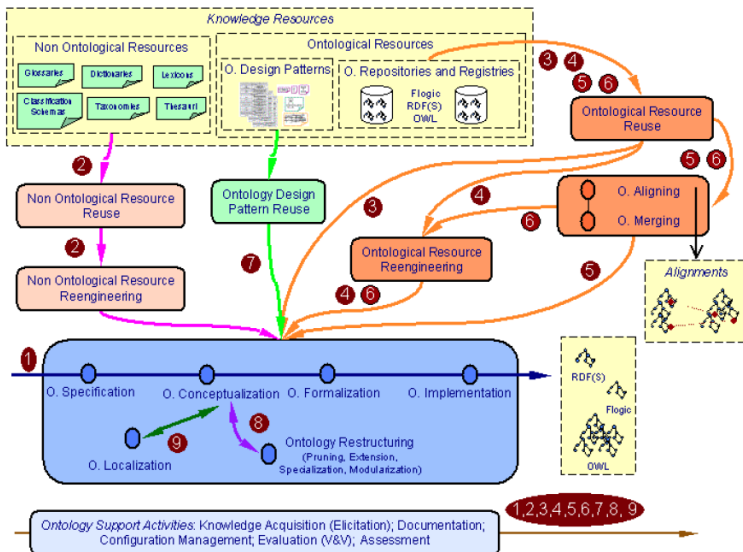
# Why ontologies?

- For their own sake, possible future use
- Representing a scientific theory precisely
- Facilitating communication among humans
- Enabling communication between software applications or modules in a complex system
- Used for and in many different ontology-driven information systems: a.o., data integration, recommender systems, NLP, textbook enhancements, Q&A systems)

# Why ontologies?

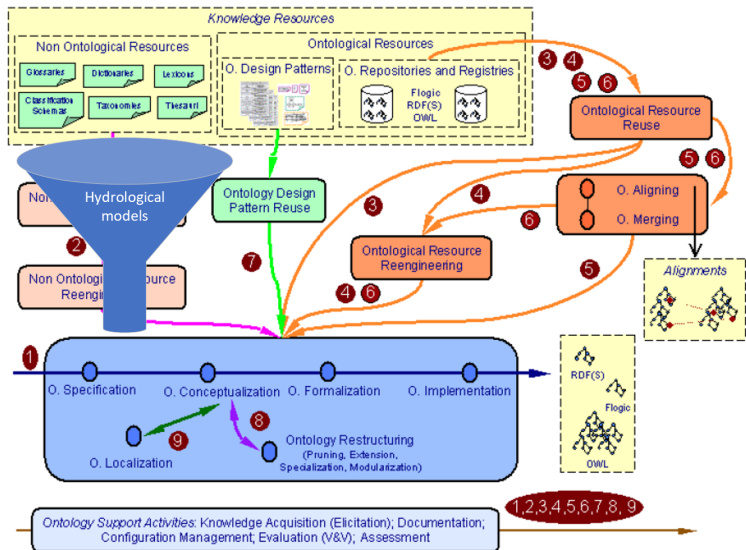
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- Examples: finding 'new' knowledge (bio-chemistry) [Wolstencroft et al.(2007)] save research time (ecology) [Madin et al.(2008)] semantic comparisons of text (healthcare) [Reese et al.(2023)], energy-optimised building system control [Pruvost and Enge-Rosenblatt(2022)] etc.

# Scenarios for building Ontology Networks (NEON methodology)

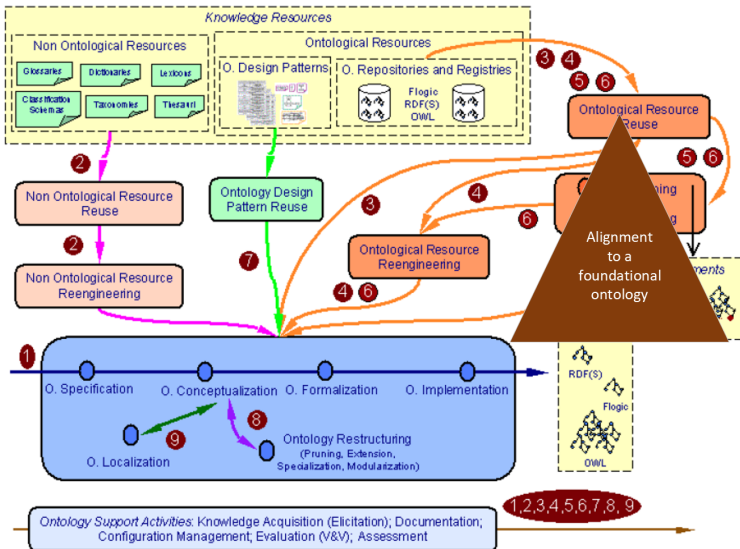




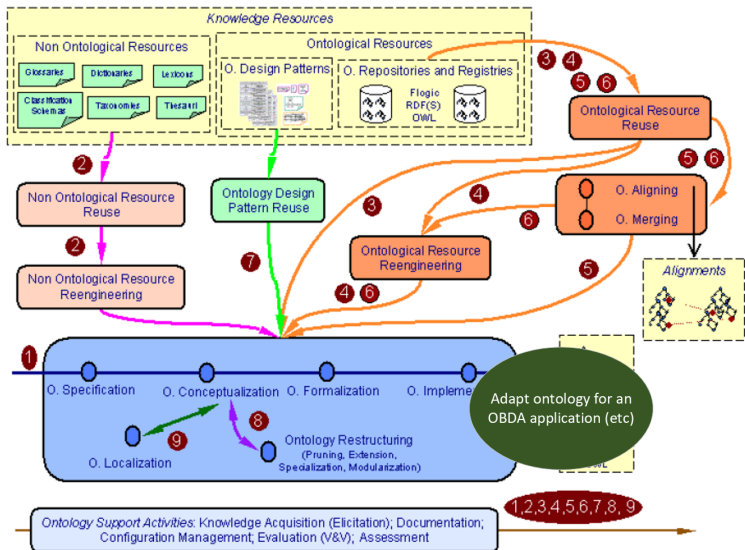
# Scenarios for building Ontology Networks (NEON methodology)



# NeOn – some extensions



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# Ontology development at the 'micro-level' level (cf. macro)

- Figure out what to add: which vocabulary and axioms
- Need to get those axioms into the ontology somehow

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- Figure out what to add: which vocabulary and axioms
- Need to get those axioms into the ontology somehow
- The actual modelling, or *ontology authoring*, using **micro-level** guidelines, methods, and tools
  - Methods, such as reverse engineering and text mining to start, OntoClean and ONTOPARTS to improve an ontology's quality
  - Tools to model, to reason, to debug, to integrate, to link to data

# Align to it – manually or assisted with D3 or BFOClassifier

BFO 2.0 Classifier

File Edit Help

OWL File:

Class Label:

Question History

Is Lion present at different times (the whole object (not only some of its parts), or is it occurring in time? (Lion  $\sqsubset$  Entity)  
Selected Answer: "Persist in time; e.g., a ball"

Can Lion exist on its own or is Lion a property of another entity or depends on at least 1 other entity (a bearer)? (Lion  $\sqsubset$  Continuant)  
Selected Answer: "Exist on its own; e.g., a sandwich"

Does Lion always have some matter (space and mass) as a part that persists in time? (Lion  $\sqsubset$  Independent Continuant)  
Selected Answer: "Always; e.g., a coffee mug"

Is Lion a collection of disjoint self-standing single objects? (Lion  $\sqsubset$  Material Entity)  
Selected Answer: "No"

Is Lion a proper part of an object, rather than a member of?

# Test-driven development

TDDonto2:

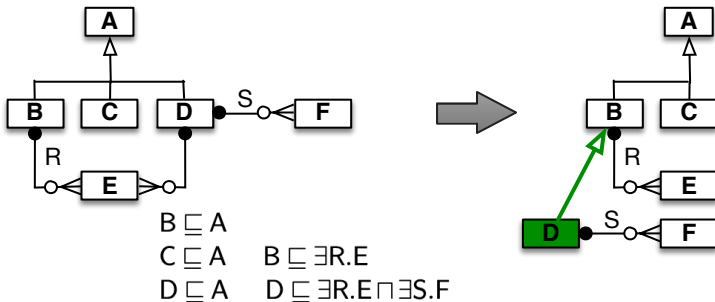
New test

PoolBraai **SubClassOf:** Pool **and** Braai

Axiom	Result
offeredBy some Accommodation SubClassOf Facility	Absent
ServiceObject EquivalentTo Attraction and Facility	Absent
ServiceObject EquivalentTo Attraction or Facility	Entailed
PoolBraai SubClassOf Braai and Pool	Incoherent

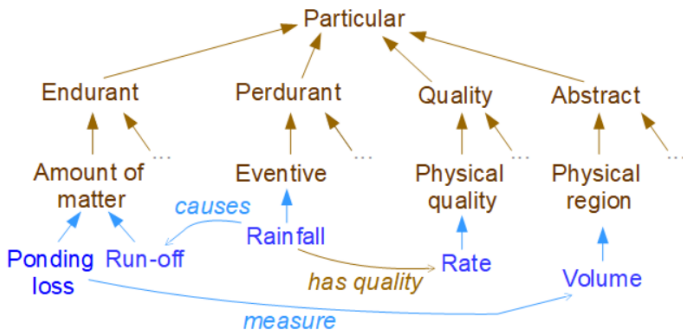
Davies K, Keet CM, Lawrynowicz A. More Effective Ontology Authoring with Test-Driven Development and the TDDonto2 tool. Int J on Artif Intell Tools, 2019.

## A note on that automated reasoning – Illustration





# Rainfall: sample \*sketch\* and some axioms for an ontology



$Rainfall \sqsubseteq Eventive$  ('rainfall is an event'),

$Rainfall \sqsubseteq \exists causes.Runoff$  ('each rainfall event causes some amount of runoff'),

$PondingLoss \sqsubseteq = 1 measure.Volume$  ('each ponding loss has exactly one measure of volume' (of the loss)),

# Limitations of ontologies?

# Limitations of ontologies?

- Yes, there are...
- ... but not part of this talk

# Feature-based comparison

**Table 7.1** Comparison of types of models along a set of properties

Model type	Feature					
	Main aim or function	Where used (mainly)	Development methodologies	Software assistance	Language freedom	Precision
Mind Maps	Basic structuring of a topic	Education, business	A little	Yes, many drawing tools	Limited	Low
Biology models	Visualise biology knowledge (structures and processes)	Biology research, textbooks	No	Drawing tools, some runtime usage (simulations)	Ranges from self-imposed to complete freedom	Low/ medium
Conceptual data models	Capture characteristics of data to be stored and processed in an program	Analysis and design stage of database and program development	Yes	Drawing tools, limited runtime usage	Ranges from standardised languages to partial freedom to design one	Medium
Ontologies	Represent knowledge of a subject domain precisely and in a computer processable way	Computing and IT (Data integration, Enterprise systems, Web search, etc.)	Yes, many	Editors (diagram, text), runtime usage	Ranges from standardised languages to partial freedom to design one	High (but medium/ low is possible)
Ontology	Characterise one small aspect of interest precisely and in much detail	Research	No	No	Yes, can define as one goes along	High/ Very high

(also from the 'what and how' book)



## Recap and future work

- Representing knowledge of the domain, semantics of the equations, declarative-imperative separation
- Different types of declarative models: diagrams, conceptual data models, ontologies
- Which one suits best depends on the task

## Recap and future work

- Representing knowledge of the domain, semantics of the equations, declarative-imperative separation
- Different types of declarative models: diagrams, conceptual data models, ontologies
- Which one suits best depends on the task
- Opportunities for declarative hydrological modelling
- Repurpose some of the design steps from computing to hydrological modelling?
- Use the resulting models for ontology and conceptual model development

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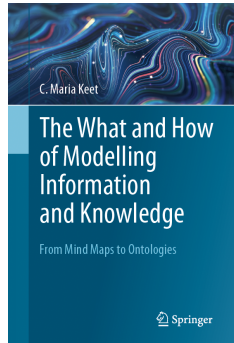




# Thank you!

## Questions?

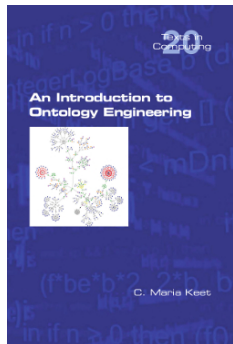
- My book on modelling,
- aimed at a broader audience, and
- available in hardcopy and eBook
- <https://link.springer.com/book/10.1007/978-3-031-39695-3>



# Thank you!

## Questions?

- My textbook on ontology engineering (aimed at computer scientists)
- Free pdf (and slides and exercises) at <https://people.cs.uct.ac.za/~mkeet/OEbook/>
- Also available in paperback (College Publications):



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